# FedCD: A Hybrid Federated Learning Framework for Efficient Training with IoT Devices

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Abstract-With billions of IoT devices producing vast data globally, privacy and efficiency challenges arise in AI applications. Federated learning (FL) has been widely adopted to train deep neural networks (DNNs) without privacy leakage. Existing centralized and decentralized FL architectures have limitations, including memory burden, huge bandwidth pressure and non-IID data issues. This paper introduces a novel hybrid FL framework, named FedCD, merging the benefits of both centralized and decentralized FL architectures. FedCD strategically distributes the model based on layer sizes and consensus distances (i.e., the deviation between the local models and the global average models), effectively relieving network bandwidth pressures and accelerating training speed even under the non-IID setting. This method significantly mitigates resource constraints and improves model accuracy, offering a promising solution to the challenges in distributed machine learning. Extensive experiment results show the high effectiveness of FedCD. The total completion time of FedCD is reduced by 16.3%-53% and the average accuracy improvement is 1.85% compared to the baselines.

*Index Terms*—Edge Computing, Federated Learning, Resource Constraints, Non-IID data, IoT Devices.

## I. INTRODUCTION

**B** ILLIONS of Internet of Things (IoT) devices globally generate substantial data, including photos and voice samples, propelling the advancement of artificial intelligence (AI) [1]. Nonetheless, the process of cloud computing carries the inherent risk of privacy breaches since the data gathered by the cloud may contain sensitive and confidential user information. Also, transferring all data to a remote cloud server can increase latency and degrade user experience [2]. Therefore, edge computing (EC) [3], [4] has emerged as a solution to locally store data and shift high computing power applications from cloud servers to network edges [5]. Furthermore, to alleviate data privacy leakage concerns, federated learning

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J. Huang is with the Anhui Province Key Laboratory of Affective Computing and Advanced Intelligence Machine and School of Computer and Information, Hefei University of Technology, Hefei, 230601, China.E-mail: hjy@hfut.edu.cn. (FL) [6], [7] is employed for distributed machine learning at the network edge across distributed datasets. Additionally, some techniques (*e.g.*, differential privacy [8], [9]) also can be adopted to enhance individual privacy by adding noise to data in FL.

The most prevalent and widely used architecture in the existing FL mechanisms is the centralized FL architecture [6], [10], which involves local training at the network edge and model aggregation at the parameter server (PS). Initially, each worker executes stochastic gradient descent (SGD) [6] on its local dataset to minimize the loss function and then dispatches the updated model to the PS for global aggregation. Subsequently, the PS circulates the averaged model back to the workers for the following round of local training. However, the PS can become a bottleneck due to potential traffic congestion caused by numerous workers simultaneously communicating, leading to system breakdown if the PS is compromised.

Decentralized federated learning (DFL) [11], [12] serves as an alternative FL architecture. Here, each worker exchanges models with its neighbors and aggregates them for the subsequent local training. As there is no central PS, DFL eliminates the likelihood of traffic congestion and failure risks at the PS. Furthermore, communication between workers is faster than between workers and the PS, significantly reducing communication time. Despite these advantages, two challenges exist in DFL: 1) Limited Memory Size. Workers must receive and store neighbor models, which may strain memory resources because the memory size of a worker is always limited. 2) Non-IID Local Data. The training data of a worker is always determined by the environment and users' preferences. The data in each worker is not independent and identically distributed (non-IID) in practice and cannot represent the overall data distribution. For example, in the garage, some cameras take more pictures of people, and some take more pictures of vehicles. This challenge also exists in centralized FL. But in DFL, each worker only exchanges models with a limited number of neighbors, and the training speed and the test accuracy are affected more by non-IID local data [13], [14].

To address the memory strain challenge raised by large model sizes, the model parallelism technique [15]- [16] is suggested. This approach divides the model into sub-models and distributes them across various devices, alleviating device resource consumption. For instance, RePurpose [15] adjusts neuron positions to decrease intermediate data transmission between workers. However, it still increases network bandwidth strain due to frequent data transmission. The pdADMM [16] divides the model by layers, allowing each layer to update the model independently without communicating with other layers. However, this method is only suitable for relatively small models. Current deep neural networks (DNNs) have large parameter sizes that continue to grow. Transmitting these large models to the PS or neighbors will inevitably consume substantial bandwidth resources, presenting a significant challenge for both centralized and decentralized architectures.

In this paper, we propose a novel hybrid FL framework, named FedCD, which combines features of both centralized and decentralized architectures, to enhance model training with IoT devices. In FedCD, we leverage the model parallelism, *i.e.*, some model layers (or sub-model) adopt centralized aggregation, while the remaining model layers adopt decentralized aggregation. Specifically, we design a score for each layer according to the layer's location and size, and distribute the layers to the PS and the neighbors according to the scores at the beginning stage. Then we use the intermediate data (*i.e.*, consensus distances [17]) to form a new layer distribution method at the following stage. FedCD relieves network bandwidth pressure by transmitting sub-models in both centralized and decentralized architectures. However, under the decentralized setup, each worker exchanges models with only a limited number of other workers, reducing model performance when local data is non-IID [14]. To address this, FedCD incorporates a centralized architecture to aggregate sub-models into a global model at the PS, yielding good performance even with non-IID local data. Furthermore, only sub-models are stored in the workers' memories which can relieve the burden of the memories. Consequently, our proposed FedCD can enhance model training even under non-IID settings and alleviate resource constraint pressures. The main contributions of our work can be summarized as follows:

- We propose a novel hybrid FL framework, called FedCD, which facilitates the distribution of sub-models to the PS and the workers' neighbors for efficient aggregation. We provide theoretical evidence affirming the convergence guarantee of model training with FedCD.
- We design a novel algorithm that strategically determines the distribution of layers to the PS and the neighbors. This decision is initially based on the sizes and positions of the layers, and it is subsequently adjusted according to consensus distances, enabling accelerated convergence speed.
- Experiment results on classical models and real-world datasets show the effectiveness of the proposed method. FedCD can accelerate the training speed by 16.3% 53% and reduce communication traffic compared to the existing FL systems.

The rest of this paper is organized as follows. Section II introduces some preliminaries, and proposes the novel framework of FedCD. We also give the convergence analysis and formalize the problem in Section II. Besides, we provide the motivation for the algorithm design and propose the efficient algorithm for FedCD in Section III. In Section IV, the experiments are conducted and the corresponding results are presented. The related works are summarized in Section V. Finally, we conclude the paper in Section VI.

## II. PRELIMINARIES AND PROBLEM FORMULATION

#### A. Federated Learning

Traditional centralized FL consists of N workers and a parameter server (PS). Each worker i has a loss function based on the local dataset  $D_i$  and the size of the dataset is  $|D_i|$ . The loss function can be defined as:

$$F_{i}(w_{i}^{t}) = \frac{1}{|D_{i}|} \sum_{\xi \in D_{i}} f_{i}(w_{i}^{t}, \xi)$$
(1)

where  $w_i^t$  is the model parameter of worker *i* at round *t* and  $\xi$  is a batch of the local dataset  $D_i$ .  $f_i(w_i^t, \xi)$  is the local loss function over  $\xi$ . To minimize the loss function  $F_i(w_i^t)$ , worker *i* uses stochastic gradient descent (SGD) [6] to update the local model, which can be formulated as:

$$w_i^{t+\frac{1}{2}} = w_i^t - \eta \nabla F_i(w_i^t) \tag{2}$$

where  $\eta$  is the learning rate,  $w_i^{t+\frac{1}{2}}$  is the local model of worker i which finishes the local training after round t, and  $\nabla F_i(w_i^t)$  is the gradient of the loss function.

After local training, each worker pushes the local model to the PS for global aggregation. This process can be formulated as:

$$F(w^{t}) = \frac{1}{N} \sum_{i=1}^{N} F_{i}(w^{t})$$
(3)

where  $w^t = \frac{1}{N} \sum_{i=1}^{N} w_i^t$  and  $F(w^t)$  is the global loss function. Then the PS sends the updated global model to the workers for the next training.

In decentralized FL, the workers are connected in a network topology. This topology can be modeled as an undirected graph G = (V, E), where  $V = \{1, 2, ..., N\}$  and  $E \in V \times V$ . We use a matrix  $A = \{A_{i,j} \in \{0, 1\}, 1 < i, j < N\}$  to represent the graph, where  $A_{i,j} = 1$  represents there is a link between worker *i* and worker *j*. Otherwise,  $A_{i,j} = 0$ . Worker *i* first updates the local model using SGD, and then sends the local model to neighbors. Worker *i* receives the models from their neighbors and aggregates them as:

$$w_i^{t+1} = w_i^t + \sum_{j \in N_i^t} u_{i,j}^t (w_j^{t+\frac{1}{2}} - w_i^{t+\frac{1}{2}})$$
(4)

where  $N_i^t$  is the neighbor set of worker *i* at round *t*.  $u_{i,j}$  is the mixing weight for aggregating the model of worker *j*. After aggregating the received models, the worker *i* adopts the aggregated model for the next local training.

## B. Overview of FedCD

In this section, we will introduce our proposed framework FedCD, which includes an edge server (PS) and some workers. In FedCD, the PS periodically receives the status information (*e.g.*, the consensus distance and the accuracy improvement). After that, the PS generates the layer distribution policy and sends it to the workers at regular intervals. Once the workers receive the policy, the workers will send some layers to the PS and send the rest layers to the neighbors according to the policy. This entire process operates over numerous communication rounds until the model achieves convergence.

We introduce more details about the training process of FedCD through the workflow in Fig. 1. Firstly, in the initialization stage of the model, PS will initialize the entire global



Fig. 1: The overview of FedCD.

model and send it to all workers. Then, workers perform local model training with the fresh global model. Subsequently, PS generates the layer distribution policy, *i.e.*, which layer sends to the PS and which layer sends to the neighbors, according to the status information and proposed algorithm in Section III. After that, the workers send some layers to the PS and send some layers to the neighbors. The PS aggregates the received models using  $w^{g,t}(l) = \frac{1}{N} w_i^t(l)$  at round t, where  $w_i^t(l)$  is the layer l of trained model at worker i. Then, PS sends the updated model  $w^{g}(l)$  to the workers. In addition, the workers will aggregate the models from the neighbors, and the aggregated model of worker i is denoted as  $w_i^{n,t}(l)$ . Finally, worker *i* performs model combination, which is defined as  $w_i^{c,t} = \{ w^{g,t}(\mathcal{L}_1), w_i^{n,t}(\mathcal{L}_2) \},$  wherein layers received from the PS are included in set  $\mathcal{L}_1$ , and those received from the neighbors are included in set  $\mathcal{L}_2$ . After combination, the worker *i* uses the combined model  $w_i^{c,t}$  for the next local training. The workers use SGD to update the models:

$$w_i^{t+1} = w_i^{c,t} - \nabla f(w_i^{c,t}) \tag{5}$$

The goal of FedCD is to minimize the loss function:

$$F(w) = \frac{1}{N} \sum_{i=1}^{N} f(w_i^{c,t})$$
(6)

To better explain FedCD, we provide an example in Fig. 2. In this system, there are five workers and one PS. At the beginning, the PS initializes the model and distributes it to five clients. For worker 3, it has three neighbors (workers 1, 2, and 4) for model exchange. According to the strategy distributed by the server, these neighbors send layers 2-4 of the model to worker 3. Besides, layer 1 of all workers is transmitted to the PS for aggregation. Then, worker 3 combined layers 2-4 from neighbors and layer 1 from the PS into a fresh local model to continue training. The entire process will continue until global convergence.

## C. Convergence Analysis

In this section, we propose the convergence analysis of FedCD and make four widely used assumptions as follows:



Fig. 2: An illustration example of FedCD.

• Assumption1: Lipschitzian gradient. The loss function  $F_i$  is with L Lipschitzian gradients, *i.e.*,

$$\|\nabla F_i(w_1) - \nabla F_i(w_2)\|^2 \le L^2 \|w_1 - w_2\|^2, \forall w_1, w_2, i$$
(5)

- Assumption2: Network connectivity. The network topology G is a connected topology.
- Assumption3: Bounded gradient variance. The variance of stochastic gradients is bounded, *i.e.*,  $E_{i \in \mathbb{C}} || \nabla E_i(w) - \nabla f_i(w; \ell) ||^2 \leq \sigma^2 \forall i w$  (6)

$$E_{\xi \in D_i} || \nabla F_i(w) - \nabla f_i(w;\xi) ||^2 \le \sigma^2, \forall i, w \qquad (6)$$

$$|E_{i \in V}|| \nabla F_i(w) - \nabla F(w)||^2 \le \varsigma^2, \forall w$$
(7)

• Assumption4: Bounded model variance. The variance between the local model and global model is bounded by  $\epsilon^2$ , *i.e.*,

$$E_{i \in V} ||w^t - w_i^t||^2 \le \epsilon^2, \forall t, i.$$
(8)

where  $w^t$  is the average of the combined model of all the workers, and  $w_i^t$  is the combined model of worker *i*.

To express the relationship between the average of the combined models and the global model when one worker finishes local training, we adopt an upper bound  $\alpha^2$ , *i.e.*,

$$||w^{t+1} - w^{t+\frac{1}{2}}||^2 \le \alpha^2 \tag{9}$$

where  $w^{t+\frac{1}{2}}$  represents the global model when one worker finishes the local training using SGD after round t, and  $w^{t+1}$ represents the average of the combined models in round t+1.

We conduct an experiment to test the change in the value of  $||w^{t+1} - w^{t+\frac{1}{2}}||$ . The results show that  $||w^{t+1} - w^{t+\frac{1}{2}}||$  oscillates around 0.8 in IID settings and around 1 in non-IID settings with the increase of communication rounds. So we can use a small bound to limit  $||w^{t+1} - w^{t+\frac{1}{2}}||^2$ .

We also define the upper bound  $\beta^2$  as:

$$||\nabla F(w^{t+\frac{1}{2}})||^2 - ||\nabla F(w^t)||^2 \le \beta^2 \tag{10}$$

We replace the parameter in [18] (e.g.,  $\hat{M}_k$  by  $\epsilon^2$ ). The detailed proof is as follows: ( $w^0$  is the initial model,  $w^*$  is the optimal model which minimizes F)

$$E[F(w^{t+2}) - F(w^{*})] \leq E[F(w^{t}) - F(w^{*})] - \frac{\eta M}{2N}E||\nabla F(w^{t})||^{2} + \lambda$$
(11)  
where  $\lambda \leq \frac{\eta M L^{2} \epsilon^{2}}{2N} + \frac{\eta^{2} L(\sigma^{2} M + 6\varsigma^{2} M^{2})}{2N^{2}} + \frac{6\eta^{2} L^{3} M^{2} \epsilon^{2}}{N^{2}}, M$  is

the size of the data used in each communication round by one worker. We further have:

$$E[F(w^{t+1}) - F(w^{t+\frac{1}{2}})]$$

$$\leq E < \nabla F(w^{t+\frac{1}{2}}), w^{t+1} - w^{t+\frac{1}{2}} > +\frac{L}{2} ||w^{t+1} - w^{t+\frac{1}{2}}||^{2}$$

$$= \frac{1}{2} ||\nabla F(w^{t+\frac{1}{2}}) + w^{t+1} - w^{t+\frac{1}{2}}||^{2} - \frac{1}{2} ||\nabla F(w^{t+\frac{1}{2}})||^{2}$$

$$- \frac{1}{2} ||w^{t+1} - w^{t+\frac{1}{2}}||^{2} + \frac{L}{2} ||w^{t+1} - w^{t+\frac{1}{2}}||^{2}$$

$$\leq \frac{1}{2} \left\{ ||\nabla F(w^{t+\frac{1}{2}})||^{2} + ||w^{t+1} - w^{t+\frac{1}{2}}||^{2} \right\}$$

$$+ \frac{L}{2} ||w^{t+1} - w^{t+\frac{1}{2}}||^{2}$$

$$\leq \frac{1}{2} E ||\nabla F(w^{t})||^{2} + \frac{1}{2}\beta^{2} + \frac{L+1}{2}\alpha^{2}$$
(12)

By adding Eq. (11) and Eq. (12), we obtain the convergence bound between two consecutive training rounds:  $E[F(w^{t+1}) - F(w^*)]$ 

$$\leq E[F(w^{t}) - F(w^{*})] - \frac{\eta M - N}{2N} E||\nabla F(w^{t})||^{2} + \lambda + \frac{1}{2}\beta^{2} + \frac{L+1}{2}\alpha^{2} E[F(w^{t+1}) - F(w^{t})] \leq -\frac{\eta M - N}{2N} E||\nabla F(w^{t})||^{2} + \lambda + \frac{1}{2}\beta^{2} + \frac{L+1}{2}\alpha^{2}$$
(13)

We sum the results in Eq. (13) from t=0 to t=T-1 and obtain:  $\sum_{t=0}^{T-1} E[F(w^{t+1}) - F(w^t)] = E[F(w^T) - F(w^0)]$ 

$$\leq -\frac{\eta M - N}{2N} \sum_{t=0}^{T-1} E ||\nabla F(w^{t})||^{2} + T\left(\lambda + \frac{1}{2}\beta^{2} + \frac{L+1}{2}\alpha^{2}\right)$$

$$\frac{1}{T} \sum_{t=0}^{T-1} E ||\nabla F(w^{t})||^{2}$$

$$\leq \frac{2N(F(w^{0}) - F(w^{*}))}{T(\eta M - N)} + \frac{2N}{(\eta M - N)}\left(\lambda + \frac{1}{2}\beta^{2} + \frac{L+1}{2}\alpha^{2}\right)$$
(14)

## D. Problem Formulation

To train models among distributed workers by FL, it is inevitable to consume resources (e.g., CPU cycles and network traffic). Formally, we define the computing resource consumption of worker k in one round as  $c_k$ . Thus, the computing resource consumption of T rounds is  $Tc_k$ . We accumulate N workers' computing consumption and the total consumption should not exceed its budget  $B_c$ . Each worker's transmission workload of centralized architecture is defined as  $W_a$ , where  $W_a = \sum_{i=1}^{L} (1 - x_i)M(i)$ . We define the total size of the transmitted data of one peer in a decentralized architecture as  $W_b$ , where  $W_b = \sum_{i=1}^{L} 2x_iM(i)$ . M(i) is the data volume of the *i*-th layer model.  $x_i$  is a binary variable and it indicates whether layer i adopts centralized architecture or not (0 for adopting centralized architecture and 1 for adopting decentralized architecture). We define the total transmission budget of a round as  $B_b$ . Let  $B_1$  and  $B_2$  represent the inbound bandwidth between workers and the PS, and the outbound bandwidth between workers and the PS, respectively. We denote the bandwidth of worker j and worker m as  $B_{jm}$ .  $r_{jm}$  is a binary variable and it indicates whether there is a link between worker j and worker m. We define the capacity budget for PS node as  $C_a$  and the capacity budget for worker j as  $C_i$ . We formulate the problem as follows:

min 
$$\lambda H + (1 - \lambda) f(w^t)$$

. . . . . .

$$s.t.\begin{cases} \sum_{k=1}^{N} Tc_k \leq B_c\\ \sum_{k=1}^{N} 2W_a + \sum_{j=1}^{N} \sum_{m=1}^{N} W_b r_{jm} \leq B_b\\ NW_a \leq C_a\\ W_b \sum_{m=1}^{N} r_{jm} \leq C_j\\ x_i = \{0, 1\}\\ r_{jm} = \{0, 1\}\end{cases}$$
(7)

Let  $H = \max \{ W_a / B_1 + W_a / B_2, \max \{ W_b / B_{jm} \} \}.$ 

Our objective is to minimize the maximum communication time and maximize the training speed of FedCD. If  $\lambda$  is set as a large number, we pursue the minimum communication time of a round. If  $\lambda$  is set as a small number, we pursue the quick training speed of a round. The first inequality indicates that the computing workload of T rounds for N workers is less than a budget. The second inequality indicates the total transmission cost per round is less than a budget. The third inequality indicates the PS node's capacity is larger than the total transmission volume between the PS node and workers. The fourth inequality indicates each worker's capacity is larger than the total sizes of the collected models of each worker.

# **III. ALGORITHM DESIGN**

# A. Motivation for the Algorithm Design

This section provides a brief description of the inspiration sources in the early stage of the research, and designs LDLS algorithms based on some experimental phenomena in the early stage. Subsequent experiments have proven that the algorithm we designed is efficient. In early experiments, we evenly distributed the CIFAR10 [19] dataset to ten clients with independent and identically distributed(iid) local data types using the AlexNet [20] model. We fixed the learning rate to 0.01 and conducted two experiments. The first experiment (case1) sent layers 0-8 to PS, layers 9-10 to neighbors, and the second experiment (case2) sent layers 0, 2, 4, 6, 8, and 10 to PS, layers 1, 3, 5, 7, and 7 were sent to neighbors to observe their aggregation and model accuracy in different rounds, and the results are shown in the figure2.

We observe that in the early stages of training (when the accuracy increases significantly), sending adjacent layers to the same target (case1), i.e. PS or neighbors, results in faster convergence speed compared to sending adjacent layers to different targets (case2). Therefore, we considered this discovery and designed the LDLS algorithm, which combines the size and position of each layer to determine whether to use CFL or DFL for each layer in the early training stage. The detailed algorithm design is shown in the following figure.

# B. Layer Distribution based on the Layer's Location and Size

We design two algorithms to decide which layer is sent to the PS and which layer is sent to the neighbors. We first introduce the layer distribution method which is based on the layers' locations and sizes in FedCD (LDLS in Alg. 1). In LDLS, worker *i* first initializes two vectors  $\mu_1$  and  $\mu_2$ , which represent the maximum time when each layer is sent to the PS and neighbors, respectively. FedCD uses  $sum_1$ and  $sum_2$  to express the total time when the layers are sent



Fig. 3: Performance of AlexNet over CIFAR-10 under two different layer allocation strategies.

to the PS or the neighbors (Line 1). FedCD also initializes the unassigned layers set  $Q_1$  which contains all the layers (Line 2). Since the network bandwidth always fluctuates, the architecture uses the average value to represent the network bandwidth. We assume that the inbound bandwidth between the workers and the PS is  $B_1$ , and the outbound bandwidth between the workers and the PS is  $B_2$ . Worker *i* computes the time when it transmits the layer *l*'s parameter from the worker to the PS and downloads it from the PS to the worker, *i.e.*,  $\mu_1(l) = M(l)/B_1 + M(l)/B_2$ . M(l) is the size of layer *l*. We define the minimum bandwidth in the network as  $B_{min}$ , the maximum time when each worker transmits the layer *l*'s parameter using the decentralized method is  $\mu_2(l) = M(l)/B_{min}$ . The layers sent to the PS are in the set  $L_1$ , and the layers sent to the neighbors are in the set  $L_2$ .

We choose the layer with the minimum element in  $\mu_1$  and the layer is named  $c_1$  (Line 4), and choose the layer with the maximum element in  $\mu_2$  and the layer is named  $c_2$  (Line 6). Then,  $c_1$  and  $c_2$  are removed from  $Q_1$  (line 7). We insert  $c_1$  and  $c_2$  to  $L_1$  and  $L_2$  respectively (Line 8). Then we add  $\mu_1(c_1)$  to  $sum_1$  (Line 9) and add  $\mu_2(c_2)$  to  $sum_2$  (Line 9).  $d_1$  is used to express the layer's distance from  $c_1$ . If the number of the layer is lower than  $c_1$ ,  $d_1$  will be lower than 0, and if the number of the layer is higher than  $c_1$ ,  $d_1$  will be higher than 0.  $d_2$  is used to express the layer's distance from  $c_2$ . Then we compute the score of each layer: We denote  $m = (\sigma_1 d_1 + \sigma_2 d_2)M(l)$ :

$$score(l) = e^m$$
 (15)

Alg. 1 introduces the LDLS method when  $c_1 < c_2$ . If  $c_1 < c_2$ , the centralized method will choose the layer with the minimum score, and the decentralized method will choose the layer with the maximum score. That is because the scores of the layers next to  $c_1$  are small and the scores of the layers next to  $c_2$  are very large. If  $sum_1 < sum_2$ , we first choose the element in  $Q_1$  with the minimum score and the layer will be named  $l_1$ . Then we move the layer  $l_1$  out of  $Q_1$  and insert  $l_1$  to  $L_1$ . And  $sum_1$  will be added by  $\mu_1(l_1)$  (Lines 11-15). If  $sum_1 > sum_2$ , we will choose the element in  $Q_1$  with the largest score and the layer will be named  $l_2$ . Then  $l_2$  will be sent to the neighbors for aggregation. We move the layer  $l_2$  out of  $Q_1$  and insert  $l_2$  to  $L_2$ . And  $sum_2$  will be added by  $\mu_2(l_2)$ (Lines 17-20). If  $c_1 > c_2$ , the centralized method will choose the layer with the maximum score, and the decentralized method will choose the layer with the minimum score. The

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| Algorithm 1 LDLS $(c_1 < c_2)$ |  |  |  |
|--------------------------------|--|--|--|
| 1:                             | Initialize $\mu_1, \mu_2, L_1, L_2, sum_1 = 0, sum_2 = 0$ ;    |  |  |
| 2:                             | Initialize the set of unassigned layers $Q_1 = \{1, 2,, L\};$  |  |  |
| 3:                             | Sort all layers in non-decreasing order by $\mu_1(l)$ ;        |  |  |
| 4:                             | Select the first element $c_1$ ;                               |  |  |
| 5:                             | Sort all layers in non-increasing order by $\mu_2(l)$ ;        |  |  |
| 6:                             | Select the first element $c_2$ ;                               |  |  |
| 7:                             | $Q_1 \leftarrow Q_1 - \{c_1\};  Q_1 \leftarrow Q_1 - \{c_2\};$ |  |  |
| 8:                             | $L_1.insert(c_1);  L_2.insert(c_2);$                           |  |  |
| 9:                             | $sum_1 + = \mu_1(c_1);  sum_2 + = \mu_2(c_2);$                 |  |  |
| 10:                            | while $Q_1 \neq \phi$ do                                       |  |  |
| 11:                            | if $sum_1 < sum_2$ then  |  |  |
| 12:                            | search the element $l_1$ with minimum score in $Q_1$ ;         |  |  |
| 13:                            | $L_1.insert(l_1);$   |  |  |
| 14:                            | $Q_1 \leftarrow Q_1 - \{l_1\};$                                |  |  |
| 15:                            | $sum_1 + = \mu_1(l_1);$  |  |  |
| 16:                            | else   |  |  |
| 17:                            | search the element $l_2$ with maximum score in $Q_1$ ;         |  |  |
| 18:                            | $L_2.insert(l_2);$   |  |  |
| 19:                            | $Q_1 \leftarrow Q_1 - \{l_2\};$                                |  |  |
| 20:                            | $sum_2 + = \mu_2(l_2)$ :                                       |  |  |

algorithm will end when all the layers are distributed.

# C. Layer Distribution based on Consensus Distance

Note that LDLS may face performance degradation when the number of workers in the network is large and the number of epochs in a communication round is small. To this end, the layer distribution based on consensus distances [17] (LDC in Alg. 2) is proposed. The consensus distance  $D^{t}(l)$  represents the deviation between the local model and the average global model of layer l. If  $D^{t}(l)$  is small, it represents that the local model is similar to the average global model and the workers don't need to send the layer l to the PS. On the contrary, if  $D^{t}(l)$  is large, it means that the local model differs greatly from the average global model, so the workers need to send layer l to the PS. We define the consensus distance of worker i is  $D^t(l) = \frac{1}{N} \sum_{i=1}^{N} D_i^t(l)$ . If the layer uses centralized method,  $D_i^{t+1}(l)$  is defined as  $D_i^{t+1}(l) = ||\bar{w}^{t+1}(l) - w_i^{t+\frac{1}{2}}(l)||$ , where  $w_i^{t+\frac{1}{2}}$  is the model of worker *i* which finishes performing local training after round t and  $\bar{w}^{t+1}(l) = \frac{1}{N} \sum_{i=1}^{N} w_i^{t+\frac{1}{2}}(l)$ . If the layer uses decentralized method,  $D_i^{t+1}(l)$  is defined as  $D_i^{t+1}(l) =$  $||\bar{w}^{t+1}(l) - w_i^{t+1}(l)||$ , where  $w_i^{t+1}(l)$  is the model of worker i which finishes aggregation using the models received from neighbors after round t. However, in DFL, the average model  $\bar{w}^{t+1}(l)$  is not available in practice. If the layer adopts a decentralized method to update the model, we will use the following method to calculate the consensus distance:  $D_{:}^{t+1}(l)$ 

$$\begin{aligned} &= \left| \left| \bar{w}^{t+1}(l) - w^{t+1}_i(l) \right| \right| \\ &= \left| \left| \frac{1}{N} \sum_{j=1}^{N} w^{t+\frac{1}{2}}_j(l) - (w^{t+\frac{1}{2}}_i(l) + \sum_{j=1}^{N} u^{t}_{i,j} A_{i,j}(w^{t+\frac{1}{2}}_j(l) - w^{t+\frac{1}{2}}_i(l))) \right| \right| \\ &= \left| \left| \sum_{j=1}^{N} \frac{w^{t+\frac{1}{2}}_j(l) - w^{t+\frac{1}{2}}_i(l)}{N} - u^{t}_{i,j} A_{i,j}(w^{t+\frac{1}{2}}_j(l) - w^{t+\frac{1}{2}}_i(l)) \right| \right| \end{aligned}$$

We set  $u_{i,i}^t = \frac{1}{N}$  for simplicity, and then  $D_i^{t+1}(l)$  is the possible maximum value, thus it follows:  $n^{t+1}$ 

$$\begin{split} &D_{i}^{++}(l) \\ &= \left| \left| \sum_{j=1}^{N} \frac{(1-A_{i,j})(w_{j}^{t+\frac{1}{2}}(l)-w_{i}^{t+\frac{1}{2}}(l))}{N} \right| \right| \\ &\leq \frac{1}{N} \sum_{j=1}^{N} (1-A_{i,j}) D_{i,j}^{t+1} \\ &\text{ where } D_{i,j}^{t+1}(l) = \left| |w_{i}^{t+\frac{1}{2}}(l) - w_{j}^{t+\frac{1}{2}}(l) | \right|, \\ &D_{i,j(max)}^{t+1}(l) \\ &= \left| |w_{i}^{t+\frac{1}{2}}(l) - w_{k}^{t+\frac{1}{2}}(l) + w_{k}^{t+\frac{1}{2}}(l) - w_{j}^{t+\frac{1}{2}}(l) | \right| \\ &\leq \left| |w_{i}^{t+\frac{1}{2}}(l) - w_{k}^{t+\frac{1}{2}}(l) | + \left| |w_{k}^{t+\frac{1}{2}}(l) - w_{j}^{t+\frac{1}{2}}(l) \right| \right| \\ &\leq \left| |w_{i}^{t+\frac{1}{2}}(l) - w_{k,j}^{t+\frac{1}{2}}(l) | + \left| |w_{k}^{t+\frac{1}{2}}(l) - w_{j}^{t+\frac{1}{2}}(l) \right| \right| \\ &= D_{i,k}^{t+1}(l) + D_{k,j}^{t+1}(l) \\ &D_{i,j(min)}^{t+1}(l) \\ &\geq \left| \left| |w_{i}^{t+\frac{1}{2}}(l) - w_{k}^{t+\frac{1}{2}}(l) | - \left| |w_{k}^{t+\frac{1}{2}}(l) - w_{j}^{t+\frac{1}{2}}(l) \right| \right| \right| \\ &\geq \left| \left| |w_{i}^{t+\frac{1}{2}}(l) - D_{k,j}^{t+\frac{1}{2}}(l) \right| \\ &= \left| D_{i,k}^{t+1}(l) - D_{k,j}^{t+1}(l) \right| \end{aligned}$$

Thus, we can estimate 
$$D_{i,j(max)}^{t}(l)$$
 as  $\hat{D}_{i,j(max)}^{t}(l)$ :  
 $\hat{D}_{i,j(max)}^{t}(l) = \min_{k \in [N] - \{i,j\}} (D_{i,k}^{t}(l) + D_{k,j}^{t}(l))$  (16)

we also can estimate  $D_{i,j(min)}^t(l)$  as  $\hat{D}_{i,j(min)}^t(l)$ :

$$D_{i,j(min)}^{t}(l) = \max_{k \in [N] - \{i,j\}} (||D_{i,k}^{t}(l) - D_{k,j}^{t}(l)||)$$
(17)

If  $D_{i,j(max)}^t(l)$  is used to calculate  $D^t(l)$ ,  $D^t(l)$  is recorded as  $D_{max}^t(l)$ .  $D_{min}^t(l)$  is the same.  $t_{ps}$  and  $t_{nb}$  represent the total time when the layers are sent to the PS and the neighbors. If  $\frac{t_{ps}}{t_{rk}}$  is low, we need to arrange more layers to adopt centralized method. Thus, the probability of transmitting layer *l* to the PS  $p_l^t$  is inversely proportional to  $\frac{t_{ps}}{t_{nb}}$ . We perform LDC when the round t=nT, where T is the interval of performing two adjacent LDC. Based on the above analysis, we determine the variable  $p_1^t$  by using the following equation:

$$p_{l}^{t} = \frac{\left[\lambda \sum_{h=(n-1)T}^{nT} D^{h+1}(l) + (1-\lambda)(e^{|d-d_{m}|})\right]e^{\frac{1}{\Delta\xi}}}{e^{\sqrt{\frac{t_{ps}}{t_{nb}}}}} \quad (18)$$

If the layer uses decentralized FL, we will compute the  $p_{l(max)}^{t}$  and  $p_{l(min)}^{t}$  with  $D_{max}^{h}(l)$  and  $D_{min}^{h}(l)$  to decide whether the layer will use centralized FL.  $\Delta \xi$  represents the average accuracy improvement of the models. The minimum  $\Delta \xi$  is set as 20%. If the accuracy improvement is lower, we will increase the  $p_l^t$  to make more layers use centralized mechanism. So we add  $e^{\frac{1}{\Delta\xi}}$  to the equation. We compute the average number of the layers using the decentralized method and denote it as  $d_m$ , and use d to represent the number of layer l. We use  $p_l^t$  to determine the probability of using the centralized method for the layer l. The layer with higher  $p_l^t$ will be preferentially chosen to use the centralized method. We use the exponential moving average to smooth the probability:

$$P_l = \varphi p_l^t + (1 - \varphi) P_l \tag{19}$$

where  $\varphi$  ( $0 \le \varphi \le 1$ ) is a hyperparameter that reflects the weight of the previous probability and the newly-computed probability. We use K to denote the number scale of  $P_1$ . For example, if  $P_l = 5 \times 10^{-4}$ , then K = -4. Let V(l) represent the communication rounds when layer l uses centralized FL. We use  $V_{max}$  to represent the total communication rounds. We use H(l) to denote the communication rounds when layer l uses the decentralized method. Since the layers that perform less centralized FL always have a high probability

# Algorithm 2 LDC

**Input:** the probability of the layers  $R_l$ ;  $T_1$ ,  $T_2$ ;  $S_1$ ,  $S_2$ **Output:**  $L_1$  and  $L_2$ .

- 1: while round t=nT do
- if  $\sum_{l \in L_1} R_l > T_1$  then  $S_1 = |L_1|;$ 2:
- 3:
- 4: else
- $S_1 = max\{S_1 1, 1\};$ 5:
- choose  $S_1$  layers in  $L_1$  with the largest  $R_l$  and these 6:  $S_1$  layers perform centralized FL (clear  $L_1$  and insert these these  $S_1$  layers to  $L_1$ ).
- if  $\sum_{l \in L_2} R_{l(max)} > T_2$  then 7:
- $S_2 = max\{|L_2|/2, 1\};$ 8:
- 9: else
- $S_2 = 0;$ 10:
- choose  $S_2$  layers in  $L_2$  and these  $S_2$  layers perform 11: centralized FL (insert these these  $S_2$  layers to  $L_1$ );
- clear  $L_2$  and add the unselected layers to  $L_2$ ; 12:

of performing centralized FL, we add a penalty item for the probability  $P_l$ . If the layer l is in  $L_1$ , we use Eq. (20) to calculate the decision variable  $R_l$ . If the layer l is in  $L_2$ , we use Eq. (21) to calculate the decision variable  $R_l$ .

$$R_l = P_l + 10^K \sqrt{ln(t+1)} \left(1 + \frac{V_{max}}{V(l) + 1}\right)$$
(20)

$$R_l = P_l + 10^K \frac{\sqrt{ln(t+1)}}{1 + V_{max} - H(l)}$$
(21)

When performing LDC (Alg. 2) for the first time, we first choose the minimum layer and choose another L- $S_1$ - $S_2$ -1 layers which are next to the minimum layer with the smallest sizes to use the decentralized method. The average number of these layers is denoted as  $d_m$ . The rest layers adopt a centralized method. When it is not the first time to perform LDC, we first sum up  $R_l$  of the layers in  $L_1$ . If the sum is larger than the threshold  $T_1$ ,  $S_1$  is set as  $|L_1|$  (Lines 2-3).  $S_1$  is the number of the layers which continue to perform centralized FL. If the sum is lower than the threshold  $T_1$ .  $S_1$ will minus 1 (Line 5). Then we choose  $S_1$  layers in  $L_1$  with the largest  $R_l$  and these  $S_1$  layers perform centralized FL (Line 7). Because the estimated values of  $D^t(l)$  of the layers in  $L_2$  differ significantly from the actual value, we will not compare them with the  $D^t(l)$  of the layers in  $L_1$  together. If we use  $p_{l(max)}^t$  to compute  $R_l$ , we denote  $R_l$  as  $R_{l(max)}$ , and if we use  $p_{l(min)}^{t'}$  to compute  $R_l$ , we denote  $R_l$  as  $R_{l(min)}$ . We sum up  $R_{l(max)}$  of the layers in  $L_2$  to compare it with the threshold  $T_2$ . If the sum is larger than  $T_2$ ,  $S_2$  is set to be  $max\{|L_2|/2, 1\}$ , otherwise  $S_2 = 0$  (Lines 8-11). And then we choose  $S_2$  layers in  $L_2$  to use the centralized method. If  $S_2$  isn't 0, we sort the layers by  $R_{l(max)}$  using descending order. If the difference between the value of the  $S_2$ -th and the  $(S_2+1)$ -th  $R_{l(max)}$  is less than a threshold, we choose  $S_2$ -1 layers with the highest  $R_{l(max)}$  and we choose one layer of the  $S_2$ -th and the  $(S_2+1)$ -th layers with higher  $R_{l(min)}$ . Otherwise, we choose  $S_2$  layers with higher  $R_{l(max)}$ , and these layers perform the centralized FL (Line 13). After that, we clear  $L_2$  and add the unselected layers to

TABLE I: The layers and size of the selected models.

| Model   | # of Layers | Size (MB) |
|---------|-------------|-----------|
| VGG-9   | 12          | 13.33     |
| VGG-16  | 21          | 128.25    |
| AlexNet | 11          | 88.78     |

 $L_2$  (Line 14). In the validation experiment, the LDC method can accelerate the training speed, but the final accuracy may be reduced. After performing LDC for some rounds, the workers will use the LDLS method to achieve higher accuracy.

# IV. EXPERIMENTS

This section introduces the experiment platform in Section IV-A. Then we describe the datasets and models in Section IV-B. We introduce the baselines and metrics for performance comparison in Section IV-C. The experiment results are presented in Section IV-D.

# A. Experiment Platform

We perform experiments on an AMAX deep learning workstation equipped with an Intel(R) Core(TM) i9-10900X CPU, 4 NVIDIA GeForce RTX 2080Ti GPUs and 128 GB RAM. On the workstation, we implement 5-10 processes to simulate 5-10 workers and implement 1 process to simulate the parameter server. The execution of each worker's model training is based on the PyTorch framework [21]. The socket library of Python [21] is used to build up communication between workers and the parameter server.

## B. Models and Datasets

The experiments are conducted on three well-known DNNs: VGG-9, VGG-16 [22] and AlexNet [20], which represent the middle-size model (VGG-9) and the large-size models (VGG-16 and AlexNet). The sizes of DNNs are 13.33MB,128.25MB and 88.78 MB, respectively, as shown in Table I. AlexNet is trained over CIFAR-10, which includes 50,000 images for training and 10,000 for testing. The images in CIFAR-10 are  $32 \times 32 \times 3$  dimensional and are labeled in 10 classes. VGG9 and VGG16 are trained over the CIFAR-100 dataset which is similar to CIFAR-10 but contains 100 classes. Then, we illustrate how to partition the training data under non-IID settings. For CIFAR-10, each class of the dataset distributes  $\chi$ data to one worker randomly, where  $\chi$  represents a percentage. The rest of the 1- $\chi$  data is equally distributed to the rest of the workers. For CIFAR-100, there are 100/N classes of the dataset that distribute  $\chi$  data to one worker, and the rest of the 1- $\chi$  data is equally distributed to the rest of the workers. We employ the SGD [6] optimizer for AlexNet, VGG-16 and VGG-9 and the learning rates are initialized as 0.01. The models are trained with a batch size of 64.

# C. Baselines and Metrics

**Baselines:** We choose three classical and efficient algorithms as baselines for performance comparison, which are summarized as follows:



Fig. 4: AlexNet over CIFAR-10 under IID setting.



Fig. 5: VGG-9 overCIFAR-100. Fig. 6: Total traffic in the network

- FedAvg [6] is a famous algorithm in federated learning in which the workers send the entire model to the parameter server and download the models after aggregation at PS.
- **D-PSGD** [23] is a famous algorithm in DFL. Each worker sends the trained model to the neighbors and each worker aggregates the models locally.
- NetMax [24] is a communication-aware DFL technique over the heterogeneous network. It enables each worker to asynchronously pull models from one peer for aggregation. The peers with higher bandwidth are selected with higher probabilities.

**Metrics:** We adopt the following metrics to evaluate the performance of our proposed FedCD and baselines.

- **Test accuracy** is the amount of the right data predicted by the model divided by the amount of all the data. It is used to test whether the method can converge or not.
- **Completion time** is the time when each worker finishes local training and model aggregation. It is used to evaluate the training speed.
- **Network traffic** is the total size of the models transmitted through the network, which is adopted to quantify the communication cost.

## D. Overall Performance

**Training Performance**: We use LDLS to test the performance of FedCD under IID settings. Fig. 4 shows the training performance of AlexNet over CIFAR-10 with 5-10 workers under IID settings. Fig. 5 shows the performance of VGG-9 over CIFAR-100. As we can see in Fig. 4-5, our proposed FedCD framework converges faster than FedAvg, D-PSGD, and NetMax. This is because FedCD sends the model to the PS and the neighbors simultaneously which can save time. Fig.



Fig. 7: AlexNet over CIFAR-10 under different non-IID levels.



6 shows the total traffic in the network when AlexNet reaches an accuracy of 70% and VGG9 reaches an accuracy of 50%. We can find out that FedCD consumes the least traffic. FedCD needs 22 rounds for AlexNet and 30 rounds for VGG9 to reach the target accuracy which uses the least rounds compared to the three baselines. In Fig. 4 we can find out that when the scale of workers becomes larger, our proposed FedCD still maintains its advantages over the baselines.

Performance on non-IID Data: We use LDLS to test the performance of FedCD under non-IID settings. In our experiments, the number of workers and epochs in a communication round is set as 8 and 20, respectively. We distribute the dataset into different Non-IID levels  $\chi$  (e.g., 30%, 50%, and 70%) as suggested in [25]. As shown in Figs. 7-8, we train AlexNet over CIFAR-10 and VGG-16 over CIFAR-100 under non-IID settings. FedCD outperforms baselines at all non-IID levels. For example, FedCD achieves an accuracy of 76.67%, when training AlexNet over CIFAR-10 with  $\chi$ =50%, which is higher than that of FedAvg (76.42%), D-PSGD (73.37%) and NetMax (73.79%). This is because FedCD combines the advantage of centralized and decentralized methods which is more robust in non-IID settings. Secondly, as  $\chi$  increases, the required completion time of each solution increases when achieving the same accuracy. However, Fig. 9 shows that FedCD is more robust without a significant increase in the completion time of AlexNet over CIFAR-10 when achieving the accuracy of 72%, compared with the baselines. For FedCD, the time consumption is 5,860.8s ( $\chi$ =30%), 6,837.6s ( $\chi$ =50%) and 7,326s ( $\chi$ =70%), while 7,000.4s, 9,116.8s, 13,349.6s for NetMax. This is because the per-epoch completion time of FedCD is much shorter than other solutions, and FedCD iterates more epochs and achieves a better performance under



a given time budget.

Performance of LDC: We conduct some experiments to test the effect of the LDC algorithm using AlexNet over CIFAR-10 with 10 workers. In Fig. 10(a), the first experiment uses the LDLS algorithm to train the model, and the second experiment combines the LDC and LDLS algorithms. For the first 15 rounds, we use the LDLS algorithm and for the rest rounds, we use the LDC method and don't change the layer distribution after 15 rounds. The third experiment uses LDLS for the first 15 rounds. For the rounds 15-30, we use LDC, and for the rounds after 30, we use the LDLS method again. We can find out in Fig. 10(a) that in the first experiment, the improvement of accuracy is very slow at the beginning, experiments 2 and 3 converge faster than experiment 1. However, the final accuracy of experiment 2 is lower than that of experiments 1 and 3. Finally, experiment 3 performs well on both training speed and final test accuracy.

We continue to conduct three experiments to test the performance of LDC. In Fig. 10(b), all the three experiments use LDLS at the beginning. In the intermediate stage, all three experiments use LDC. Experiment 1 changes the layer distribution at rounds 15 and 30. Experiment 2 changes the layer distribution at rounds 15, 30, and 45. Experiment 3 changes the layer distribution at rounds 10, 20, and 30. We continue to use the LDLS method after round 45 in experiment 1, round 60 in experiment 2 and round 40 in experiment 3. We can observe in Fig. 10(b) that experiment 3 converges faster than its two counterparts at the beginning, however, its training speed falls behind after 50 rounds and the final test accuracy is the lowest in the three experiments. Experiment 1 converges faster than its two counterparts after round 50 and it reaches the highest test accuracy in the end. Thus the number of training sections of LDC (when to change the layer distribution) is essential to achieve quick training speed and high test accuracy.

The Generalization of FedCD: We try to explore FedCD's performance in more applications, such as Human Activity Recognition, which is to identify a person's status (*e.g.*, standing, sitting) based on the sensor data from IoT devices (*e.g.*, smartphones or smartwatches). For this task, we adopt the HAR dataset [26] collected from 30 individuals, including 7,352 training samples and 2,947 test samples across 6 categories. The model trained on HAR is a CNN model (denoted as CNN-H) with three 5×5 convolutional layers and two fully-connected layers. We test the training performance of FedCD



Fig. 11: Training performance under different resource budgets.

and baselines under different resource (*e.g.*, completion time and network bandwidth) budgets. As shown in Fig. 11, FedCD always outperforms the baselines in terms of test accuracy. For example, given the bandwidth budget of 900MB, the accuracy of FedCD is about 64.5%, while that of NetMax, D-PSGD and FedAvg is about 62.2%, 60.7% and 58.6%, respectively. In other words, FedCD can improve the accuracy by about 2.3%, 3.8% and 5.9%, respectively. Thus, our proposed framework FedCD is also applicable to other applications.

## V. RELATED WORKS

In the past few years, FL, which possesses unique advantages in terms of privacy protection, has gradually become a hot topic [6]. This has sparked profound research by numerous scholars in the field of FL. To address the FL challenges in various application scenarios, both centralized federated learning and decentralized federated learning have been proposed, offering additional possibilities for advancements in the FL domain.

## A. Centralized Federated Learning

The concept of Centralized Federated Learning (CFL) was initially introduced [27] by Google in 2016, and subsequently, McMahan and others developed the FedAvg algorithm [6]. CFL is currently the most extensively researched and widely used FL method. Specifically, in CFL, clients at the network edge locally train the models using their respective datasets. After a certain number of local training rounds, clients send the aggregated model over the network link to a central parameter server. The server collects parameters from different clients and completes the global model aggregation. In the subsequent training round, the updated global model is sent back to specific or all clients. CFL enables collaboration in training without revealing individual client data. However, challenges such as potential network link delays, data heterogeneity [14] among different clients, and device heterogeneity [28] still require further research in this technology. Yang et al. [29] propose an iterative algorithm to address the problem of energy-efficient transmission and computation resource allocation in centralized FL. Luo et al. [30] developed an adaptive client sampling algorithm to mitigate the impact of data heterogeneity and structural heterogeneity on centralized FL. Liet al. [31] explored the impact of global aggregation rate and client weight on centralized FL.

# B. Decentralized Federated Learning

The concept of decentralized FL emerged after centralized FL. The primary goal of introducing this concept is to avoid potential network congestion and failure risks at the central server in centralized FL. By shifting communication from the client to the server to between clients, it further reduces communication costs and enhances communication efficiency. However, decentralized FL has many problems, such as posing greater challenges to the memory of workers (in some cases edge devices). Roy et al. [32] designed BrainTorrent based on the idea of decentralized federated learning, providing a highly dynamic peer-to-peer environment for clients to interact directly without relying on the central server. Hu et al. [33] proposed a segmented gossip approach, which fully utilizes the bandwidth between workers, avoiding dependence on highly concentrated topologies. Li et al. [34] proposed the BFLC framework, which combines blockchain technology with federated learning to implement a decentralized FL method that can effectively reduce consensus computation and malicious attacks.

# C. Hybrid Federated Learning

As we can see, both centralized federated learning and decentralized federated learning have their own advantages and disadvantages, so it is extremely important to find a balance between the two. However, there is little research on the combination of centralized federated learning and decentralized federated learning in existing work, and most of the work focuses on improving and analyzing these two types separately. Lalitha et al. [35] proposed the Fully Decentralized Federated Learning and analyzed the advantages of decentralized federated learning compared to traditional federated learning algorithms. Chou et al. [36] designed a framework called fed P2P, which divides the network into multiple P2P networks and only allows some devices to communicate with the PS. Beltrán et al. [37] analyzed the existing framework of DFL, reviewed its application scenarios and studied the main aspects differentiating DFL and CFL. Our proposed FedCD framework, which combines the methods of CFL and DFL, adopts different strategies to determine the aggregation method of the current layer (sent to PS or neighbors) based on the position and consensus distance of the layers. This has achieved better training performance and aggregation speed during the experimental process, providing a new idea for the combination of CFL and DFL.

## VI. CONCLUSION

In this paper, we propose a FL framework named FedCD, which is a combination of centralized and decentralized architectures. The method addresses the challenges of the memory burden, huge bandwidth pressure, and non-IID local data. We have further proposed two algorithms to decide which layer is sent to the PS and which layer is sent to the neighbors. The experiment results show that FedCD significantly outperforms baselines.

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